# Operating a Generator Paralleled to the Grid

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http://doerry.org/norbert/MarineElectricalPowerSystems/index.htm

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#### Introduction

- The steady state operation of a generator connected to a grid is different than when it is operating standalone
- Standalone
  - Voltage Regulator controls the voltage at the terminals
  - Speed Governor controls the frequency
- Paralleled to grid
  - Voltage Regulator controls the Reactive Power supplied by the generator
  - Speed Governor controls the Real Power supplied by the generator

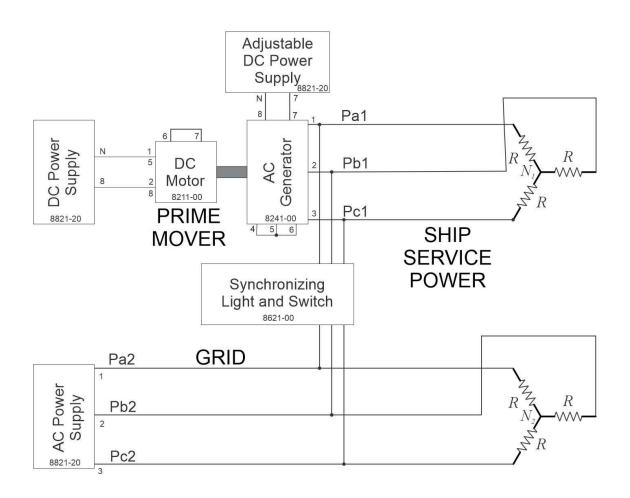
### Purpose of this video

- Using a DC Motor to represent a prime mover and an AC synchronous generator ....
  - Demonstrate how field excitation on the DC motor and on the AC Generator control speed (Frequency) and voltage when the generator is not paralleled to the grid
  - Demonstrate how field excitation on the DC motor and on the AC Generator control Real and Reactive Power when the generator is paralleled to the grid.

### Schematic

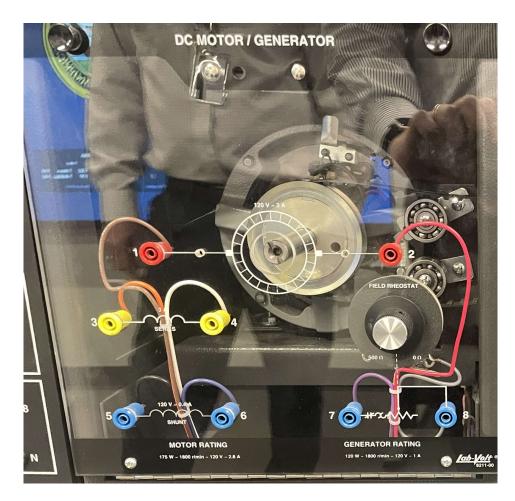
#### **Power Meter**

- Output of AC Generator
   Voltage / Frequency Meters
- Output of AC Generator
- Output of AC Power Supply



#### Prime Mover

- Modeled by a DC motor
  - Constant DC Voltage applied to the Armature (Rotor) {1 and 2}
  - Field Rheostat controls current to the Shunt Winding on the stator (Field)
    - Shunt winding {5 and 6}
    - Field Rheostat {7 and 8}
    - Connected in series
      - DC voltage {5 and 8}
      - Series connection {6 and 7}



### Steady State DC Motor Theory

$$V_a = K i_F \omega_m$$

Where  $\omega_m$  is the angular speed of the motor shaft.

$$V_{DC} - V_a = i_a R_a$$
$$T = K i_F i_a$$

Where *T* is the Torque on the motor shaft.

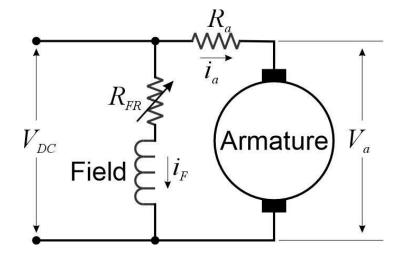
$$P = T\omega_m = V_a i_a = K i_F \omega_m i_a$$

$$P = K i_F \omega_m \frac{V_{DC} - K i_F \omega_m}{R_a}$$

For a given  $i_F$ , as power increases,  $\omega_m$  decreases.

If P is fixed, then  $i_F$  controls  $\omega_m$ 

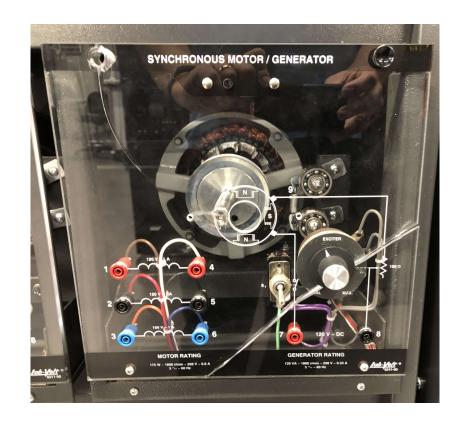
If  $\omega_m$  is fixed, then  $i_F$  controls P



In a real prime mover If P is fixed, the speed governor controls  $\omega_m$  If  $\omega_m$  is fixed, then fuel throttle controls P

#### AC Generator

- Stator windings configured in "wye"
  - One end of each coil is connected together
  - Line to line voltage is  $\sqrt{3}$  times the line to neutral voltage
  - Provides output power
- DC current in the field (rotor)
   winding controls the voltage on the
   stator windings when not
   paralleled
  - Current in the field winding is controlled by the exciter rheostat



## Steady State AC Synchronous Generator Theory

$$E_{af} = K_{rs}\omega I_F$$

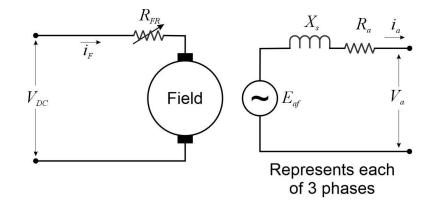
The electrical frequency  $\omega$  is proportional to the mechanical frequency  $\omega_m$ 

The total Apparent Power for all three phases is given in phasor notation (using rms values)

$$S = 3\hat{V}_a\hat{\imath}_a^* = P + Q\hat{\jmath}$$

Neglecting the losses in  $R_a$ , the power on the shaft is simply P.

$$\hat{E}_{af} = X_s \hat{\imath}_a \hat{\jmath} + R_a \hat{\imath}_a + \hat{V}_a$$



## Steady State AC Synchronous Generator Theory – Not connected to the grid

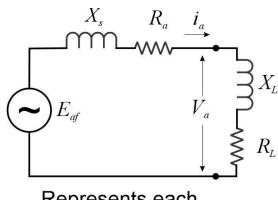
$$\hat{E}_{af} = X_s \hat{\imath}_a \hat{\jmath} + R_a \hat{\imath}_a + \hat{V}_a$$

$$\hat{V}_a = X_L \hat{\imath}_a \hat{\jmath} + R_L \hat{\imath}_a$$

$$\hat{V}_a = \frac{X_L \hat{\jmath} + R_L}{(X_L + X_S)\hat{\jmath} + (R_L + R_a)} \hat{E}_{af}$$

If the field excitation current and frequency stays constant, then as the load impedance decreases (Load apparent power increases), then the phase voltage also decreases. (Assumes shaft speed is regulated by the prime mover) Field excitation current  $I_F$  can be adjusted to maintain phase voltage.

$$E_{af} = K_{rs}\omega I_F$$



Represents each of 3 phases

### Steady State AC Synchronous Generator Theory – Connected to the grid

$$(R_a + X_S \hat{\jmath})\hat{\imath}_a = E_{af} - v_a \angle \delta_a$$

$$(R_a + X_S \hat{\jmath})\hat{\iota}_a = E_{af} - v_a \cos(\delta_a) - v_a \sin(\delta_a)\hat{\jmath}$$

$$S = 3V_a i_a^* = P + Q\hat{j} = 3|V_a||i_a| \angle \theta$$

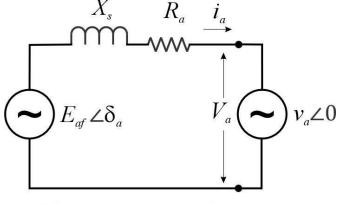
For P to be a constant,  $|i_a|\cos(\theta)$  must be a constant (since  $|V_a|$  is constant – grid voltage)

$$|i_a| \propto \frac{1}{\cos(\theta)}$$

$$E_{af} = K_{rs}\omega I_F$$

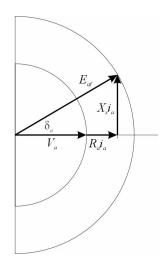
 $E_{af}$  is controlled by  $I_F$  since  $\omega$  is a constant

Angle	Power	(Power
(degrees)	Factor	Factor)^-1
0	1.000	1.000
10	0.985	1.015
20	0.940	1.064
30	0.866	1.155
40	0.766	1.305
45	0.707	1.414

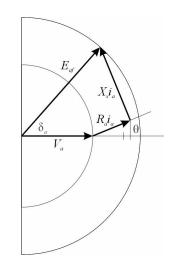


Represents each of 3 phases

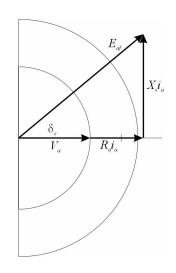
## Steady State AC Synchronous Generator Theory – Connected to the grid



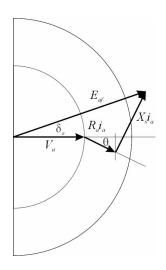
Baseline Case
Supplying
Unity Power Factor
(PF = 1.0)



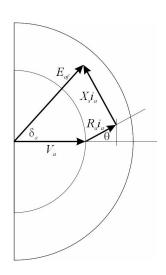
Increased Excitation on DC Motor Same  $E_{af}$  Power Increases Power Factor supplies Leading Loads



Increased Excitation on DC Motor Increased  $E_{a\!f}$  Supplying Unity Power Factor (PF = 1.0)



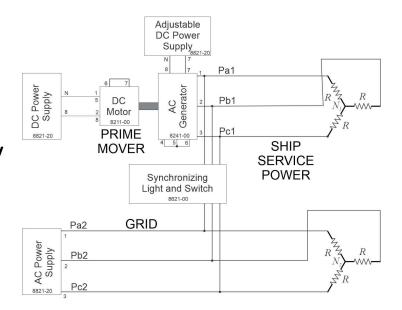
Baseline Excitation on DC Motor Increased  $E_{af}$  Supplying Lagging Loads



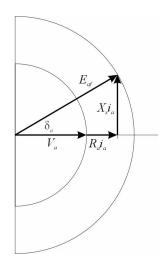
Baseline Excitation on DC Motor Decreased  $E_{af}$  Supplying Leading Loads

#### Procedure –Paralleled

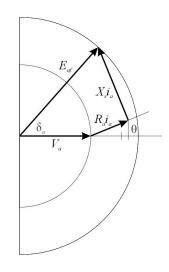
- Parallel Generator to the Grid
  - Adjust Excitation on AC Generator to supply unity power factor
- Increase excitation on DC Motor
  - Measure Real and Reactive Power
- Adjust excitation on AC Generator to supply Unity Power Factor
  - Measure Real and Reactive Power
- Increase excitation on AC Generator
  - Measure Real and Reactive Power
- Decrease excitation on AC Generator
  - Measure Real and Reactive Power



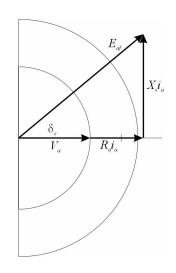
## Steady State AC Synchronous Generator Theory – Connected to the grid



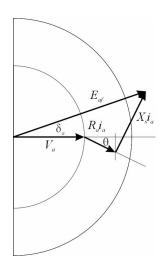
Baseline Case
Supplying
Unity Power Factor
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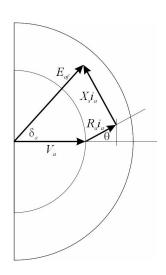
Increased Excitation on DC Motor Same  $E_{af}$  Power Increases Power Factor supplies Leading Loads



Increased Excitation on DC Motor Increased  $E_{a\!f}$  Supplying Unity Power Factor (PF = 1.0)



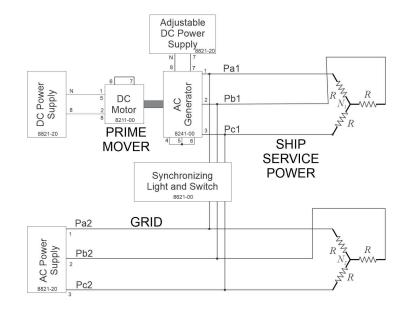
Baseline Excitation on DC Motor Increased  $E_{af}$  Supplying Lagging Loads



Baseline Excitation on DC Motor Decreased  $E_{af}$  Supplying Leading Loads

#### Procedure – Not Paralleled

- Adjust excitation to achieve 60 Hz and 208 volts line-toline with 1200 ohm Load
  - Measure Real and Reactive Power (should be about 12 watts per phase)
- Turn on 300 and 1200 ohm resistors for the load
  - Measure Real and Reactive Power (should be less than 60 watts per phase)
  - Measure Frequency and voltage (should be less than 60 Hz, and 208 volts)
- Adjust DC motor field excitation to return to 60 Hz.
  - Measure Real and Reactive Power (should be closer to 60 watts per phase)
  - Measure Frequency and voltage (should be 60 Hz and closer to 208 volts)
- Adjust AC Generator field excitation to return to 208 volts line-to-line
  - Measure Real and Reactive Power (Should be closer to 60 watts per phase)
  - Measure Frequency and voltage (Should be a little less than 60 Hz and 208 volts)



### Wrap Up